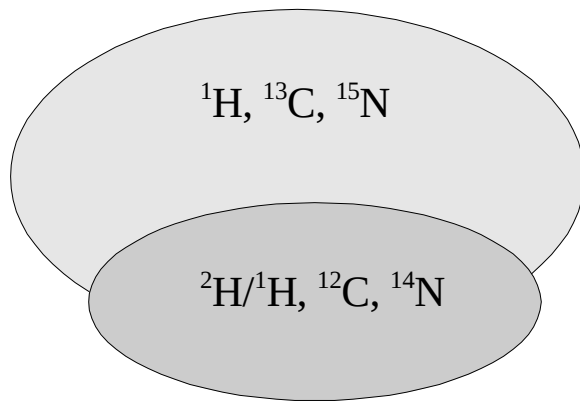
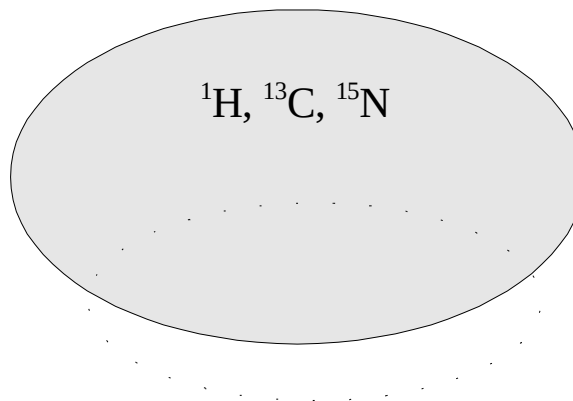


## Structural characterization of complexes using NOESY experiments

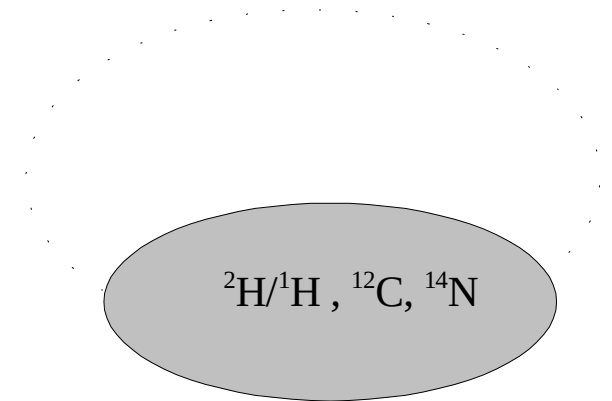
Isotope labeling ( $^{13}\text{C}$ ,  $^{15}\text{N}$ ) allows observation of individual components of a (binary) complex)



Complex with different labeling  
of the components



Isotope edited NMR spectra



Isotope filtered NMR spectra

## Basic terminology

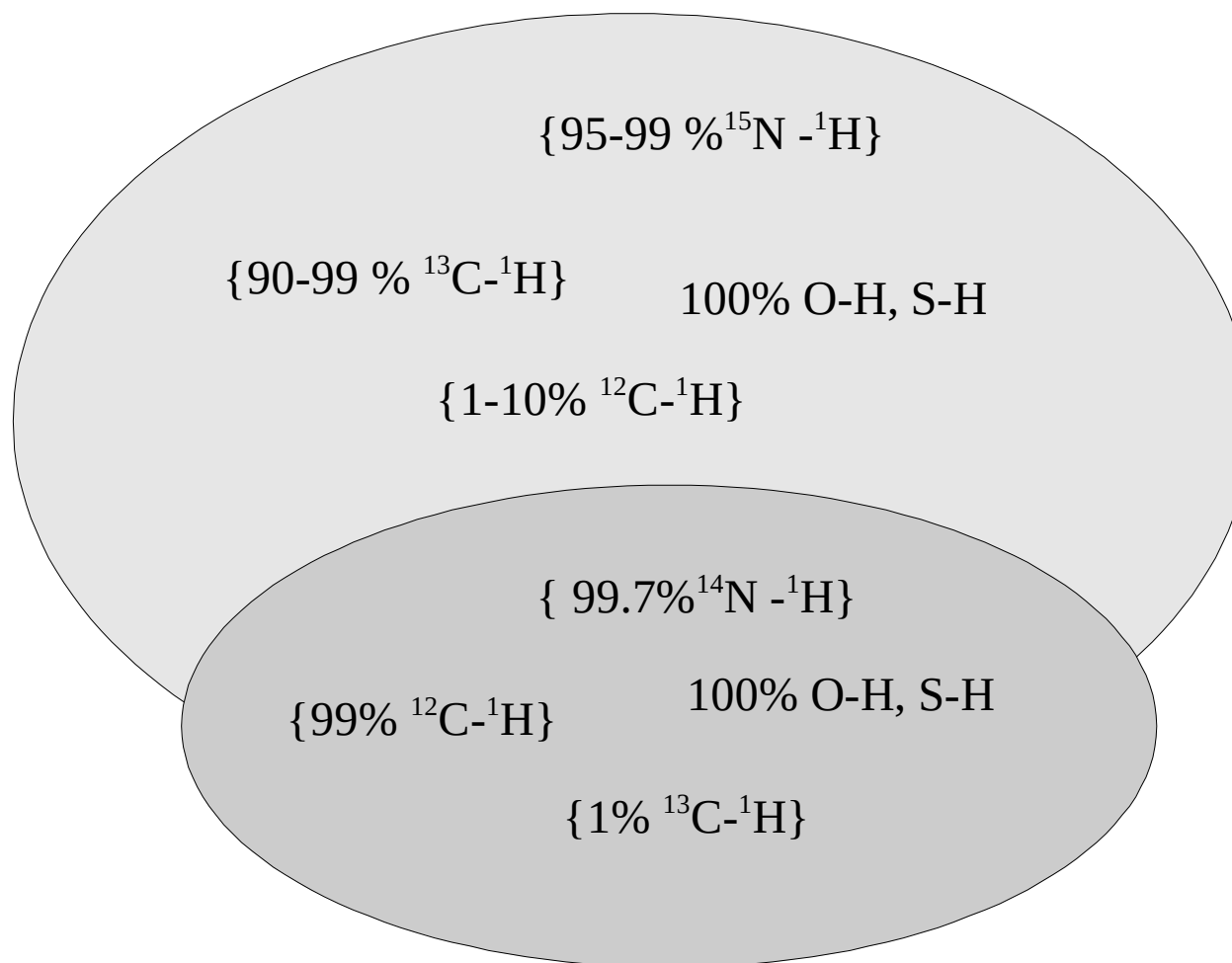
|                    |                                                                                                                                                                                                                                                    |
|--------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| Isotope editing:   | selection of protons directly bound to a NMR active heteronucleus (e.g. $^{13}\text{C}$ - $^1\text{H}$ or $^{15}\text{N}$ - $^1\text{H}$ )                                                                                                         |
| Isotope filtering: | suppression of protons directly bound to a NMR active heteronucleus,<br>ideal suppression corresponds to the 'selection' of protons bound to NMR 'inactive' nuclei<br>(e.g. $^{12}\text{C}$ - $^1\text{H}$ , $^{14}\text{N}$ - $^1\text{H}$ , O-H) |

## Important isotopes for biomolecular NMR

| NMR active isotope | natural abundance | corresponding NMR inactive isotope | natural abundance |
|--------------------|-------------------|------------------------------------|-------------------|
| $^1\text{H}$       | 99.985 %          | $^2\text{H}$                       | 0.015 %           |
| $^{13}\text{C}$    | 1.11 %            | $^{12}\text{C}$                    | 98.9 %            |
| $^{15}\text{N}$    | 0.37 %            | $^{14}\text{N}$                    | 99.63%            |

( $^{14}\text{N}$ ,  $^2\text{H}$  are quadrupol nuclei, relaxes very fast in biomacromolecules, nearly NMR inactive)

In practice: real isotope composition of complexes (in H<sub>2</sub>O solution)



## Selectivity for isotope editing

$$\text{Selectivity} = \frac{\text{Fraction of wanted observed component}}{\text{Fraction of unwanted observed component}}$$

$$\text{Sel.}_{\text{Iso.Ed.}} = \frac{\text{concentration(labeled component)} * \text{degree of labeling}}{\text{concentration(unlabeled component)} * (\text{natural abundance})}$$

$$\text{Sel.}_{\text{Iso.Filt.}} = \frac{\text{concentration(unlabeled component)}}{\text{concentration(labeled component)} * (\text{fraction of protons not bound to a NMR active heteronucleus})}$$

## Examples for the selectivity in a 1:1 complex

| Degree of $^{13}\text{C}$ labeling | selektivität <sub>Iso.Ed.</sub> | selektivität <sub>Iso.Filt.</sub> |
|------------------------------------|---------------------------------|-----------------------------------|
| 50 %                               | 50                              | 2                                 |
| 90 %                               | 90                              | 10                                |
| 99 %                               | 99                              | 100                               |

—————► Isotope filtering requires a very high degree of isotopic labeling

especially for NOESY experiments, because the relative intensity of different NOESY cross peaks show up factors in the range 10-100 (strong and weak NOE cross peaks !)

## Basic principle for isotope filtering and editing

$${}^1\text{H} - \text{X}: \quad \text{H}_x \xrightarrow{\pi {}^1J_{\text{HX}} 2\text{H}_y\text{X}_z t} \text{H}_x \cos(\pi {}^1J_{\text{HX}} t) + 2\text{H}_y\text{X}_z \sin(\pi {}^1J_{\text{HX}} t)$$

$${}^1\text{H}: \quad \text{H}_x \xrightarrow{t} \text{H}_x$$

Isotope editing: Selection of the term  $2\text{H}_y\text{X}_z$

Isotope filtering: Suppression of the term  $2\text{H}_y\text{X}_z$  and of the term  $\text{H}_x$  for the  ${}^1\text{HX}$  pairs

—————▶ Additional requirements on filtering compared to editing

## Basic principle for isotope editing

$$H_x \xrightarrow{\pi^1 J_{HX} 2H_z X_z t} H_x \cos(\pi^1 J_{HX} t) + 2H_y X_z \sin(\pi^1 J_{HX} t)$$

Maximizing of the  $2H_y X_z$  term by setting  $t = 1 / (2 J_{HX})$

$$\text{A: } H_x \cos(\pi^1 J_{HX} t) + 2H_y X_z \sin(\pi^1 J_{HX} t) \xrightarrow{\pm 90^\circ H_x} H_x \cos(\pi^1 J_{HX} t) \pm 2H_z X_z \sin(\pi^1 J_{HX} t)$$

Alternating of receiver phase eliminates  $H_x$  term

$$\text{B: } H_x \cos(\pi^1 J_{HX} t) \pm 2H_z X_z \sin(\pi^1 J_{HX} t) \xrightarrow{\pm 90^\circ X_y} H_x \cos(\pi^1 J_{HX} t) \pm 2H_z X_x \sin(\pi^1 J_{HX} t)$$

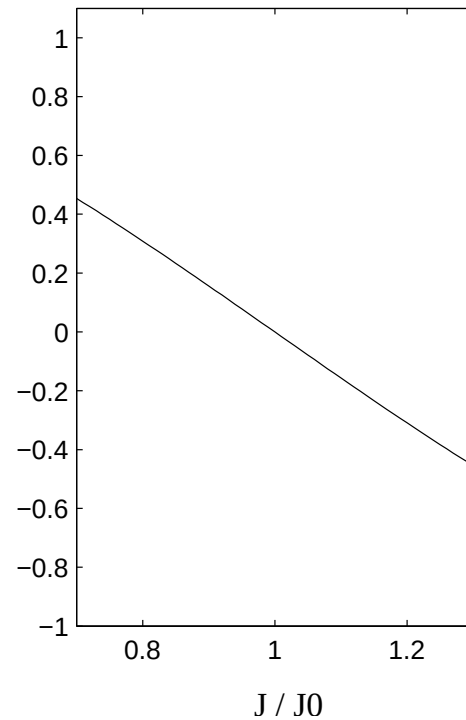
Alternating of receiver phase eliminates  $H_x$  term

—► At least one of both phase alternations is found in every phase cycling of an isotope edited experiment (e.g. HSQC) !

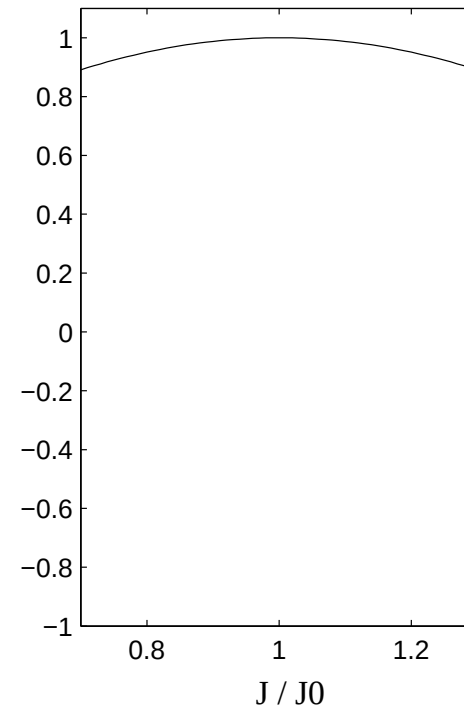
## Dependence on the relative size of the J-coupling

$$H_x \xrightarrow{\pi^1 J_{HX} 2H_z X_z t} H_x \cos(\pi^1 J_{HX} t) + 2H_y X_z \sin(\pi^1 J_{HX} t)$$

$$J_0 = 140 \text{ Hz} \longrightarrow t = 3.57 \text{ ms}$$



$$y = \cos(\pi^1 J_{HX} t)$$

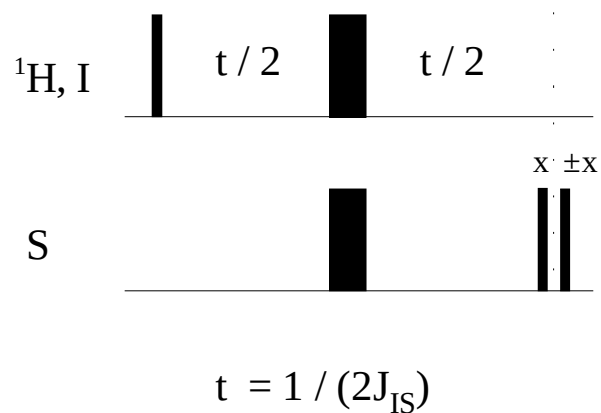


$$y = \sin(\pi^1 J_{HX} t)$$

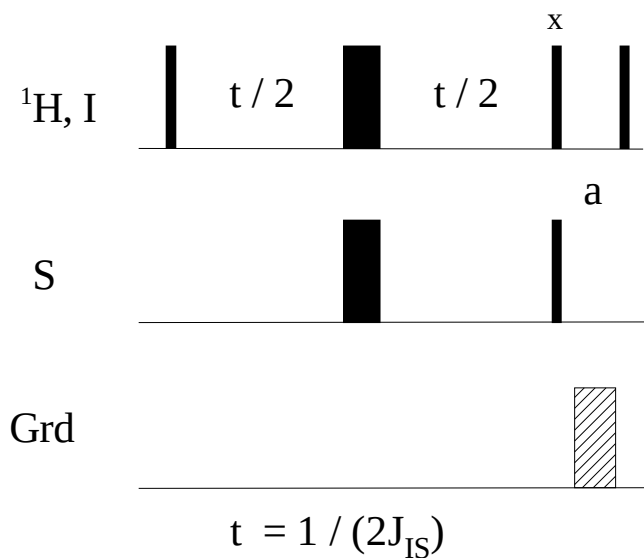
→ Intensity of the  $H_x$ -term is more sensitive to variations of the  $^1J$  couplings  
that means: Isotope filtering is more difficult compared to editing



## Examples for filtering and editing

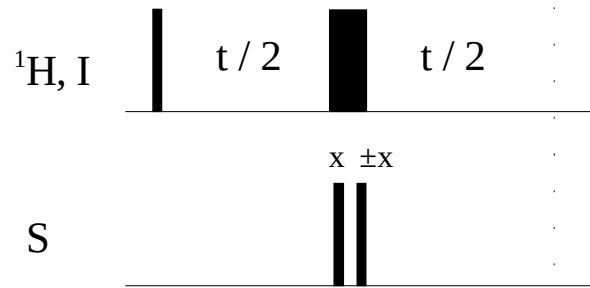


$$\begin{array}{llll}
 H_z & \text{---} & \text{---} & \longrightarrow H_y \\
 I_z & \text{---} & \text{---} & \longrightarrow I_y \cos(\pi J_{\text{IS}}t) \pm 2I_x S_z \sin(\pi J_{\text{IS}}t) \\
 \text{Receiver} & & + / + & \text{Filtering} \\
 \text{Receiver} & & + / - & \text{Editing}
 \end{array}$$



$$\begin{array}{llll}
 H_z & \text{---} & \text{---} & \longrightarrow H_z \longrightarrow -H_y \\
 I_z & \text{---} & \text{---} & \longrightarrow I_z \cos(\pi J_{\text{IS}}t) + 2I_x S_y \sin(\pi J_{\text{IS}}t)
 \end{array}$$

Dephasing by gradients



$$t = 1 / (J_{IS})$$

$$\begin{array}{lcl} H_z & \text{---} & \longrightarrow H_y \\ I_z & \text{---} & \longrightarrow I_y \cos^2(\pi J_{IS}t/2) \pm (-I_y) \sin^2(\pi J_{IS}t/2) \end{array}$$

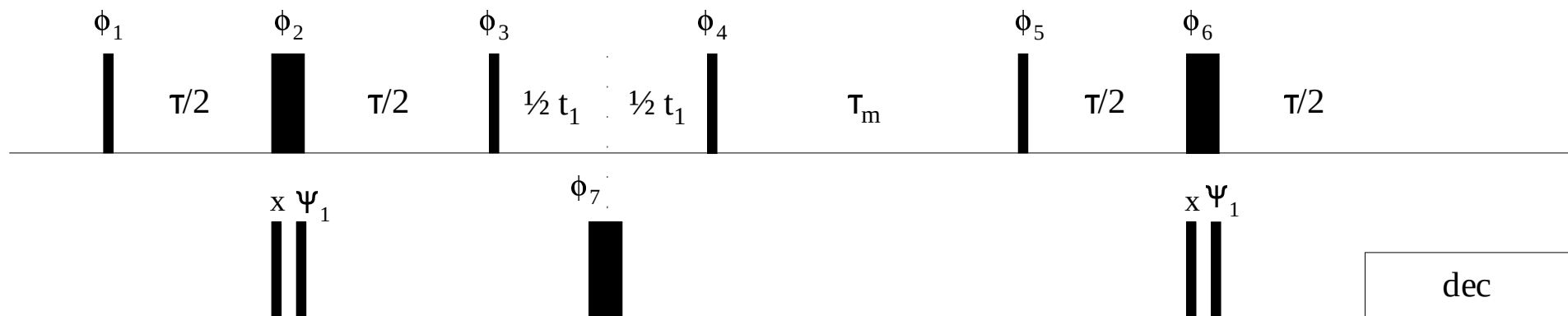
$$H_z \xrightarrow{(90^\circ_x - t/2 - 180^\circ_x - t/2)} H_y$$

$$I_z \xrightarrow{(90^\circ_x - t/2)} -I_y \cos(\pi J_{IS}t/2) + I_x S_z \sin(\pi J_{IS}t/2)$$

$$-I_y \cos(\pi J_{IS}t/2) + I_x S_z \sin(\pi J_{IS}t/2) \xrightarrow{(180^\circ_x(I) + 90^\circ_x(S) + 90^\circ_{\pm x}(S))} I_y \cos(\pi J_{IS}t/2) \pm (-I_x S_z) \sin(\pi J_{IS}t/2)$$

$$I_y \cos(\pi J_{IS}t/2) \pm (-I_x S_z) \sin(\pi J_{IS}t/2) \xrightarrow{(t/2)} I_y \cos^2(\pi J_{IS}t/2) \pm (-I_y) \sin^2(\pi J_{IS}t/2)$$

# Inclusion of half filters in a NOESY experiment (G. Otting, K. Wüthrich (1989) J. Magn. Res. 85, 586-594)



$$\phi_1 = x, -x$$

$$\phi_2 = x$$

$$\phi_3 = 2\{x\}, 2\{-x\}$$

$$\phi_4 = 4\{x\}, 4\{-x\}$$

$$\phi_5 = 8\{x\}, 8\{-x\}$$

$$\phi_6 = x$$

$$\phi_7 = x$$

$$\text{rec} = x, -x, -x, x, -x, x, x, -x, -x, x, x, -x, -x, x, -x, x$$

Four subspectra

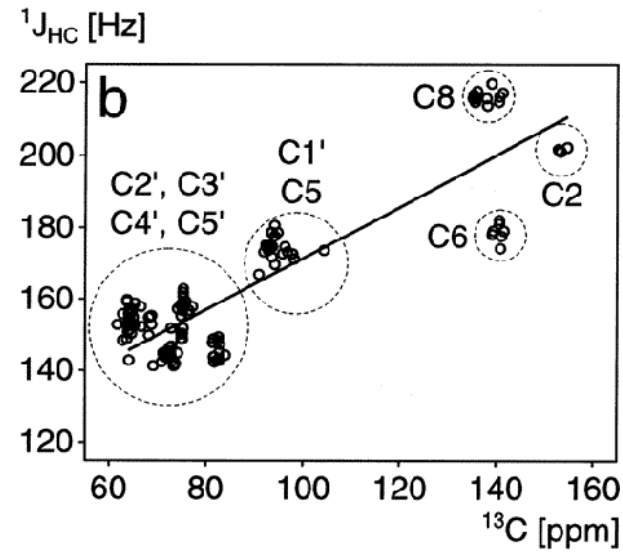
|     | $\psi_1$ | $\psi_2$ |
|-----|----------|----------|
| I   | x        | x        |
| II  | -x       | x        |
| III | x        | -x       |
| IV  | -x       | -x       |

|             |     | F1                                                    | F2                                                    |
|-------------|-----|-------------------------------------------------------|-------------------------------------------------------|
| Subspectrum | I   | $^{12}\text{C-}^1\text{H} - ^{13}\text{C-}^1\text{H}$ | $^{12}\text{C-}^1\text{H} - ^{13}\text{C-}^1\text{H}$ |
|             | II  | $^{12}\text{C-}^1\text{H} + ^{13}\text{C-}^1\text{H}$ | $^{12}\text{C-}^1\text{H} - ^{13}\text{C-}^1\text{H}$ |
|             | III | $^{12}\text{C-}^1\text{H} - ^{13}\text{C-}^1\text{H}$ | $^{12}\text{C-}^1\text{H} + ^{13}\text{C-}^1\text{H}$ |
|             | IV  | $^{12}\text{C-}^1\text{H} + ^{13}\text{C-}^1\text{H}$ | $^{12}\text{C-}^1\text{H} + ^{13}\text{C-}^1\text{H}$ |

|                          |                       | F1                         | F2                         |
|--------------------------|-----------------------|----------------------------|----------------------------|
| Linear combinations<br>→ | (I + II) + (III + IV) | $^{12}\text{C-}^1\text{H}$ | $^{12}\text{C-}^1\text{H}$ |
|                          | (I + II) - (III + IV) | $^{12}\text{C-}^1\text{H}$ | $^{13}\text{C-}^1\text{H}$ |
|                          | (I - II) + (III - IV) | $^{13}\text{C-}^1\text{H}$ | $^{12}\text{C-}^1\text{H}$ |
|                          | (I - II) - (III - IV) | $^{13}\text{C-}^1\text{H}$ | $^{13}\text{C-}^1\text{H}$ |

# $^1J(^1\text{H}, ^{13}\text{C})$ Couplings in nucleic acids and proteins

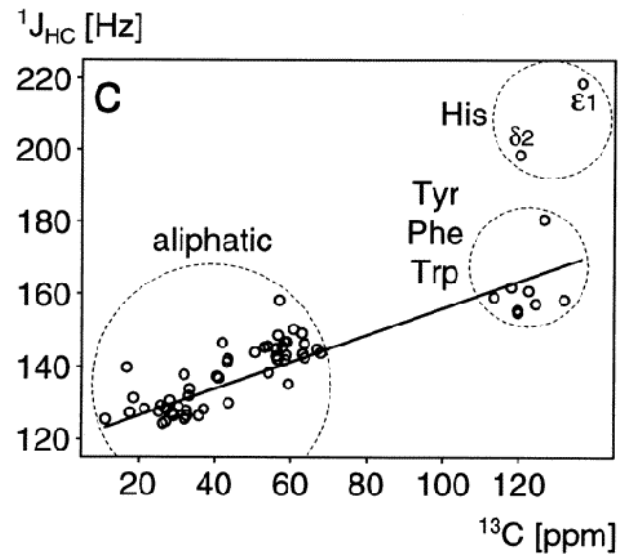
Nucleic acids



linear regression

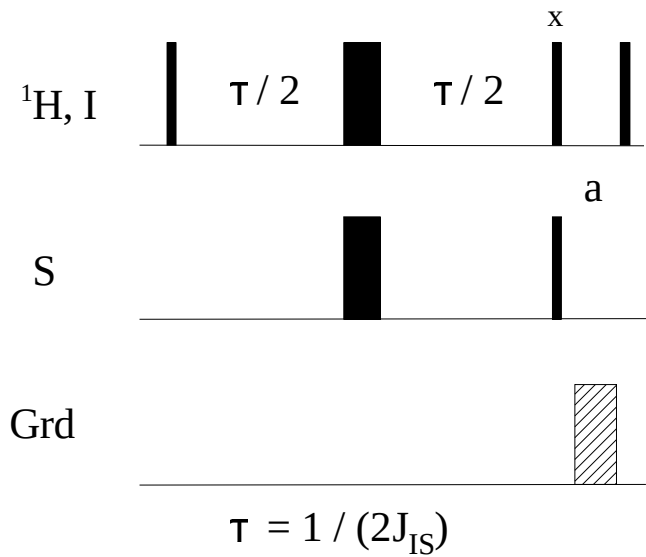
$$^1J_{\text{CH}} = 0.71(\text{Hz/ppm}) \delta_{\text{C}} + 101 \text{ Hz}$$

Proteins

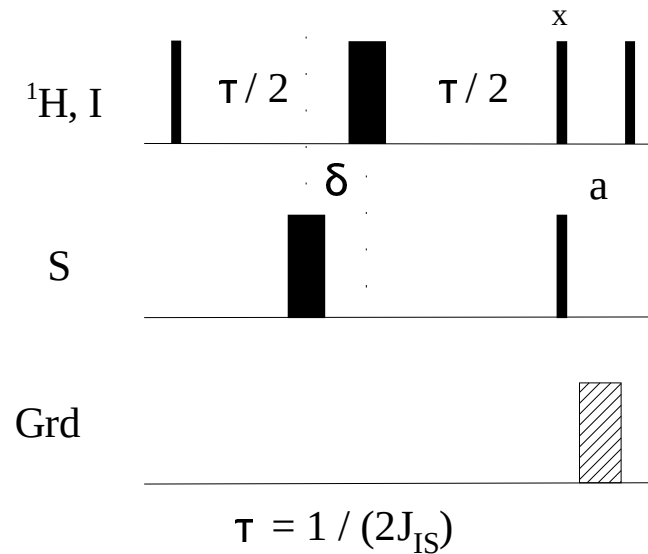


$$^1J_{\text{CH}} = 0.365 (\text{Hz/ppm}) \delta_{\text{C}} + 120 \text{ Hz}$$

# Problem with the variation of the $^1J$ couplings

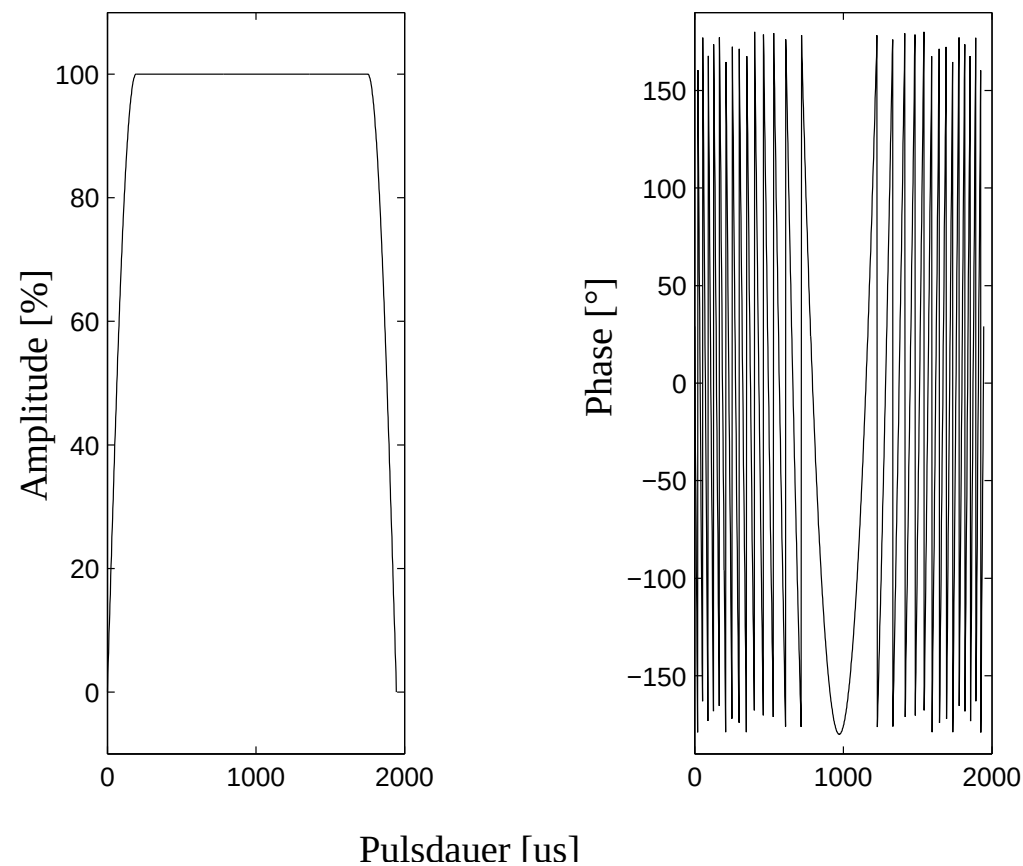
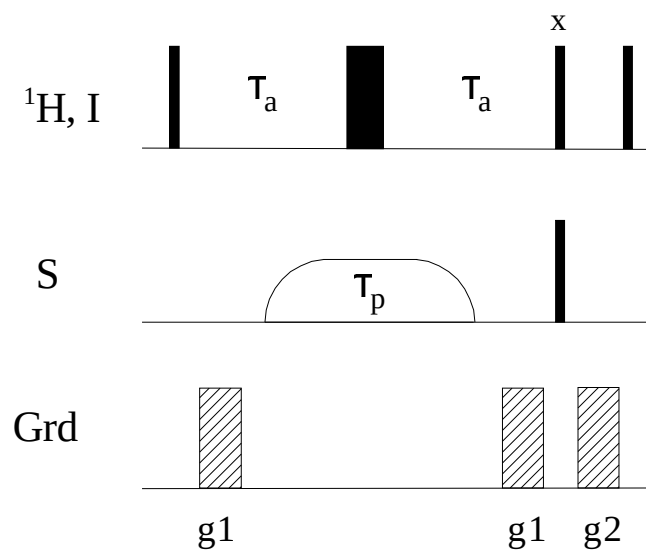


→ no ideal  $\tau$  can be found



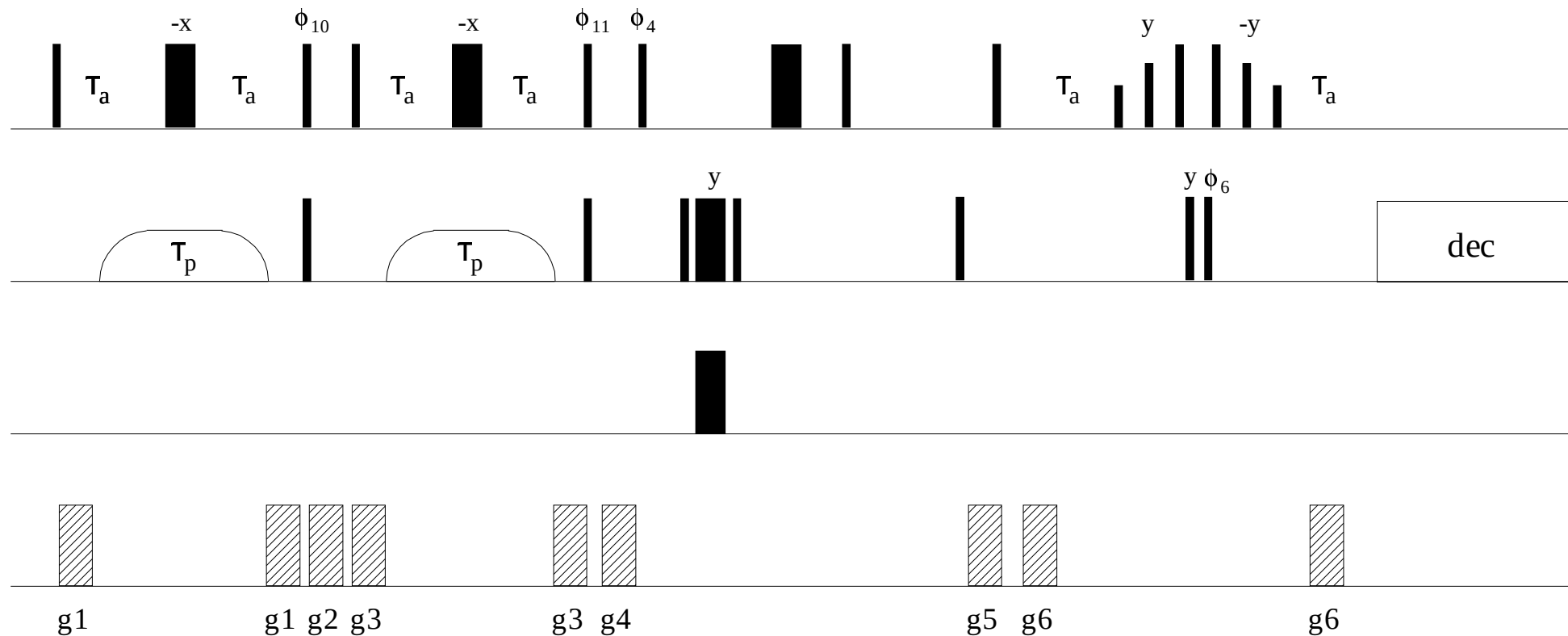
Evolution of the  $J_{IS}$ -coupling:  $\tau - 2\delta$

# Filterelement with an adiabatic S inversion pulse (C. Zwaalen et al. (1997), J. Am. Chem. Soc. 119, 6711-6721)



Puls duration      1.948 ms (800 MHz)  
smoothed chirp (10 %)  
40 kHz sweep (low-field -> high-field)

# Pulse sequence for a F1(<sup>13</sup>C-filtered)-F2(<sup>13</sup>C-edited) NOESY



$$\phi_4 = 2\{x\}, 2\{-x\}$$

$$\phi_6 = x, -x$$

$$\phi_{10} = 4\{x\}, 4\{-x\}$$

$$\phi_{11} = 8\{x\}, 8\{-x\}$$

$$rec = x, -x, -x, x, -x, x, x-, -x, -x, x, -x, -x, x, -x, x$$

$$g1 = 13 \% \quad (500 \text{ ms})$$

$$g2 = 40 \% \quad (1 \text{ ms})$$

$$g3 = 0.6 \% \quad (500 \text{ ms})$$

$$g4 = 0.1 \% \quad (1 \text{ ms})$$

$$g5 = 13 \% \quad (1 \text{ ms})$$

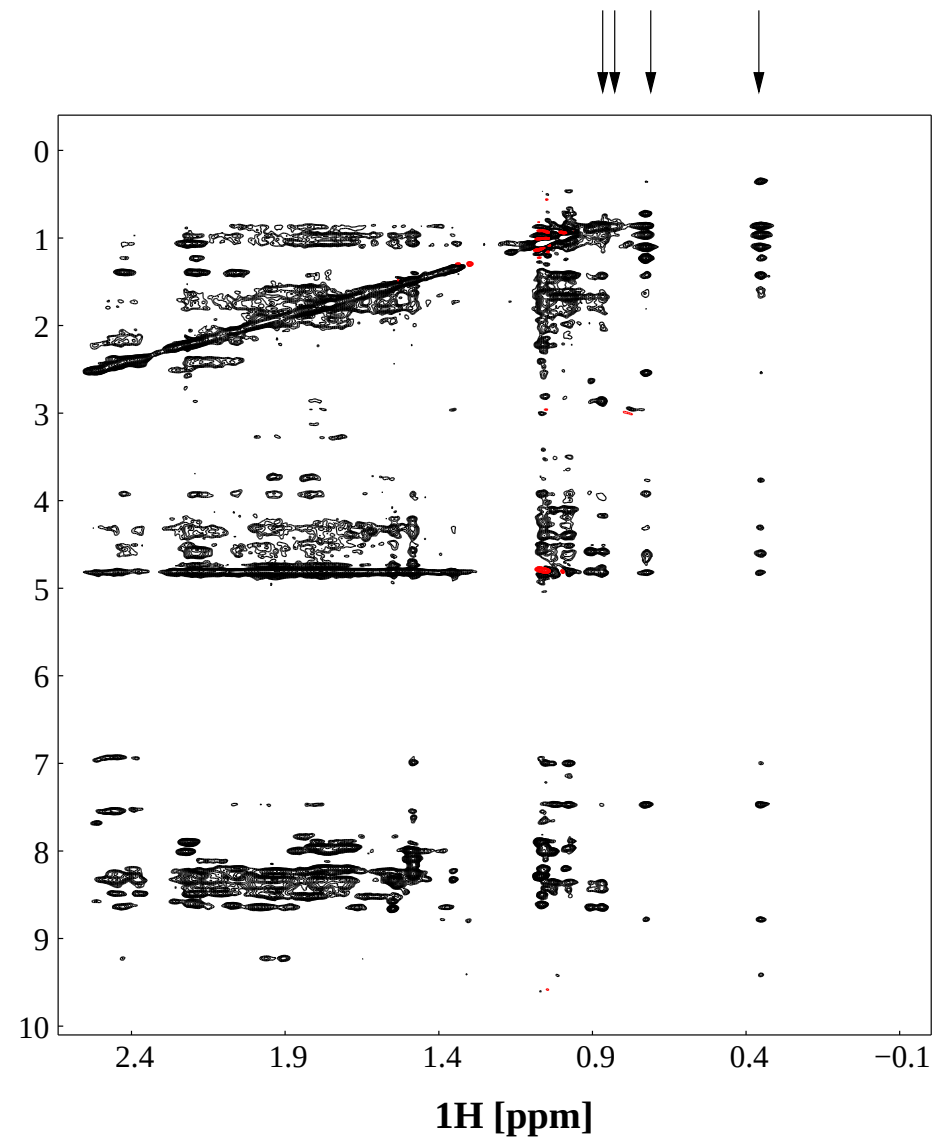
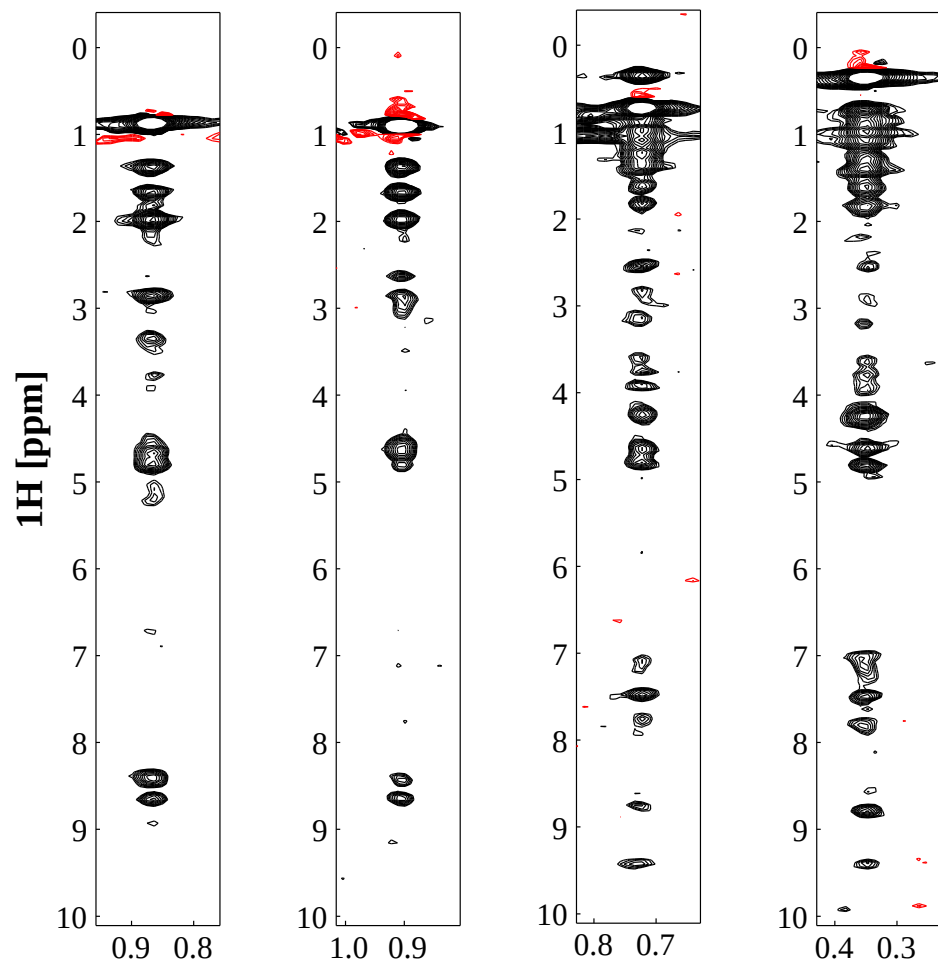
$$g6 = 50 \% \quad (1 \text{ ms})$$



F1( $^{13}\text{C}$ -filtered)-F2( $^{13}\text{C}$ -edited) NOESY of a protein-protein complex  
 $^{13}\text{C}$ ,  $^{15}\text{N}$  l N(1-53) in complex with NusA(339-495) (1:2) (l N ca. 1 mM, 800 MHz, 66 h)

Ausschnitte aus dem  $^{13}\text{C}$ -editierten NOESY

F1( $^{13}\text{C}$ -filtered) – F2 ( $^{13}\text{C}$ -edited) NOESY



1D slices from the F1( $^{13}\text{C}$ -filtered)-F2( $^{13}\text{C}$ -edited) NOESY  
compared with the  $^{13}\text{C}$ -NOESYHSQC

